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# Optimization Modeling with LINGO

Sixth Edition

LINDO Systems, Inc.



Service in China

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# Contents

<b>Contents</b> .....	<b>iii</b>
<b>Preface</b> .....	<b>xiii</b>
Acknowledgments.....	xiii
<b>1</b> .....	<b>1</b>
<b>What Is Optimization?</b> .....	<b>1</b>
1.1 Introduction.....	1
1.2 A Simple Product Mix Problem.....	1
1.2.1 Graphical Analysis .....	2
1.3 Linearity .....	5
1.4 Analysis of LP Solutions.....	6
1.5 Sensitivity Analysis, Reduced Costs, and Dual Prices.....	8
1.5.1 Reduced Costs .....	8
1.5.2 Dual Prices.....	8
1.6 Unbounded Formulations .....	9
1.7 Infeasible Formulations .....	10
1.8 Multiple Optimal Solutions and Degeneracy .....	11
1.8.1 The “Snake Eyes” Condition.....	13
1.8.2 Degeneracy and Redundant Constraints.....	15
1.9 Nonlinear Models and Global Optimization .....	16
1.10 Problems.....	18
<b>2</b> .....	<b>21</b>
<b>Solving Math Programs with LINGO</b> .....	<b>21</b>
2.1 Introduction.....	21
2.2 LINGO for Windows, Apple Mac, and Linux.....	21
2.2.1 LINGO Menu .....	23
2.2.2 Windows Menu .....	24
2.2.3 Help Menu.....	24
2.2.4 Summary.....	25
2.3 Getting Started on a Small Problem.....	25
2.4 Integer Programming with LINGO .....	26
2.4.1 Warning for Integer Programs .....	28
2.5 Solving an Optimization Model.....	28
2.6 Problems.....	29
<b>3</b> .....	<b>31</b>
<b>Analyzing Solutions</b> .....	<b>31</b>
3.1 Economic Analysis of Solution Reports.....	31
3.2 Economic Relationship Between Dual Prices and Reduced Costs.....	31
3.2.1 The Costing Out Operation: An Illustration .....	32
3.2.2 Dual Prices, LaGrange Multipliers, KKT Conditions, and Activity Costing .....	33
3.3 Range of Validity of Reduced Costs and Dual Prices .....	34
3.3.1 Predicting the Effect of Simultaneous Changes in Parameters—The 100% Rule .....	39
3.4 Sensitivity Analysis of the Constraint Coefficients.....	40
3.5 The Dual LP Problem, or the Landlord and the Renter .....	41

3.6 Problems.....	43
<b>4.....</b>	<b>49</b>
<b>The Model Formulation Process.....</b>	<b>49</b>
4.1 The Overall Process .....	49
4.2 Approaches to Model Formulation.....	50
4.3 The Template Approach .....	50
4.3.1 Product Mix Problems.....	50
4.3.2 Covering, Staffing, and Cutting Stock Problems.....	50
4.3.3 Blending Problems .....	50
4.3.4 Multiperiod Planning Problems .....	51
4.3.5 Network, Distribution, and PERT/CPM Models .....	51
4.3.6 Multiperiod Planning Problems with Random Elements.....	51
4.3.7 Financial Portfolio Models.....	51
4.3.8 Game Theory Models .....	52
4.4 Constructive Approach to Model Formulation .....	52
4.4.1 Example .....	53
4.4.2 Formulating Our Example Problem .....	53
4.5 Choosing Costs Correctly.....	54
4.5.1 Sunk vs. Variable Costs.....	54
4.5.2 Joint Products .....	56
4.5.3 Book Value vs. Market Value.....	57
4.6 Common Errors in Formulating Models.....	59
4.7 The Nonsimultaneity Error.....	61
4.8 Debugging a Model .....	61
4.9 Problems.....	63
<b>5.....</b>	<b>67</b>
<b>The Sets View of the World .....</b>	<b>67</b>
5.1 Introduction .....	67
5.1.1 Why Use Sets? .....	67
5.1.2 What Are Sets?.....	67
5.1.3 Types of Sets .....	68
5.2 The SETS Section of a Model .....	68
5.2.1 Defining Primitive Sets.....	68
5.2.2 Defining Derived Sets .....	69
5.2.3 Summary.....	70
5.3 The DATA Section .....	71
5.4 Set Looping Functions.....	73
5.4.1 @SUM Set Looping Function .....	74
5.4.2 @MIN and @MAX Set Looping Functions .....	75
5.4.3 @FOR Set Looping Function.....	76
5.4.4 Nested Set Looping Functions.....	77
5.5 Set Based Modeling Examples.....	77
5.5.1 Primitive Set Example.....	78
5.5.2 Dense Derived Set Example.....	81
5.5.3 Sparse Derived Set Example - Explicit List .....	83
5.5.4 A Sparse Derived Set Using a Membership Filter .....	88
5.6 Domain Functions for Variables .....	92

5.7 Spreadsheets and LINGO .....	92
5.8 Programming in LINGO .....	96
5.8.1 Building Blocks for Programming.....	96
5.8.2 Generating Graphs and Charts.....	98
5.9 Problems.....	100
<b>6.....</b>	<b>101</b>
<b>Product Mix Problems .....</b>	<b>101</b>
6.1 Introduction .....	101
6.2 Example.....	102
6.3 Process Selection Product Mix Problems .....	105
6.4 Problems.....	110
<b>7.....</b>	<b>113</b>
<b>Covering, Staffing &amp; Cutting Stock Models.....</b>	<b>113</b>
7.1 Introduction .....	113
7.1.1 Staffing Problems.....	114
7.1.2 Example: Northeast Tollway Staffing Problems.....	114
7.1.3 Additional Staff Scheduling Features.....	116
7.2 Cutting Stock and Pattern Selection.....	117
7.2.1 Example: Cooldot Cutting Stock Problem.....	118
7.2.2 Formulation and Solution of Cooldot .....	119
7.2.3 Generalizations of the Cutting Stock Problem .....	123
7.2.4 Two-Dimensional Cutting Stock Problems .....	125
7.3 Crew Scheduling Problems .....	126
7.3.1 Example: Sayre-Priors Crew Scheduling.....	126
7.3.2 Solving the Sayre/Priors Crew Scheduling Problem .....	128
7.3.3 Additional Practical Details .....	131
7.4 A Generic Covering/Partitioning/Packing Model .....	132
7.5 Problems.....	134
<b>8.....</b>	<b>145</b>
<b>Networks, Distribution and PERT/CPM.....</b>	<b>145</b>
8.1 What's Special About Network Models.....	145
8.1.1 Special Cases .....	148
8.1.2 Fitting into Network Structure: Roads with No Left Turns.....	148
8.2 PERT/CPM Networks and LP.....	149
8.3 Activity-on-Arc vs. Activity-on-Node Network Diagrams.....	154
8.4 Crashing of Project Networks .....	155
8.4.1 The Cost and Value of Crashing.....	156
8.4.2 The Cost of Crashing an Activity .....	156
8.4.3 The Value of Crashing a Project.....	156
8.4.4 Formulation of the Crashing Problem .....	157
8.5 Resource Constraints in Project Scheduling .....	160
8.6 Path Formulations.....	162
8.6.1 Example .....	163
8.7 Path Formulations of Undirected Networks.....	164
8.7.1 Example .....	165
8.8 Double Entry Bookkeeping: A Network Model of the Firm .....	167
8.9 Extensions of Network LP Models.....	168

8.9.1 Multicommodity Network Flows .....	169
8.9.2 Reducing the Size of Multicommodity Problems .....	170
8.9.3 Multicommodity Flow Example .....	170
8.9.4 Fleet Routing and Assignment.....	173
8.9.5 Fleet Assignment .....	176
8.9.6 Leontief Flow Models .....	180
8.9.7 Activity/Resource Diagrams.....	184
8.9.8 Spanning Trees.....	186
8.9.9 Steiner Trees .....	188
8.10 Nonlinear Networks .....	192
8.11 Problems.....	195
<b>9.....</b>	<b>203</b>
<b>Multi-period Planning Problems .....</b>	<b>203</b>
9.1 Introduction .....	203
9.2 A Dynamic Production Problem.....	205
9.2.1 Formulation .....	205
9.2.2 Constraints.....	206
9.2.3 Representing Absolute Values.....	208
9.3 Multi-period Financial Models.....	209
9.3.1 Example: Cash Flow Matching .....	209
9.4 Financial Planning Models with Tax Considerations .....	213
9.4.1 Formulation and Solution of the WSDM Problem .....	214
9.4.2 Interpretation of the Dual Prices .....	215
9.5 Present Value vs. LP Analysis.....	216
9.6 Accounting for Income Taxes .....	217
9.7 Dynamic or Multi-period Networks.....	220
9.8 End Effects .....	222
9.8.1 Perishability/Shelf Life Constraints .....	223
9.8.2 Startup and Shutdown Costs .....	223
9.9 Non-optimality of Cyclic Solutions to Cyclic Problems .....	223
9.10 Problems.....	229
<b>10.....</b>	<b>233</b>
<b>Blending of Input Materials .....</b>	<b>233</b>
10.1 Introduction .....	233
10.2 The Structure of Blending Problems.....	234
10.2.1 Example: The Pittsburgh Steel Company Blending Problem .....	235
10.2.2 Formulation and Solution of the Pittsburgh Steel Blending Problem.....	236
10.3 A Blending Problem within a Product Mix Problem .....	238
10.3.1 Formulation .....	239
10.3.2 Representing Two-sided Constraints.....	240
10.4 Proper Choice of Alternate Interpretations of Quality Requirements .....	243
10.5 How to Compute Blended Quality .....	246
10.5.1 Example .....	246
10.5.2 Generalized Mean.....	247
10.6 Interpretation of Dual Prices for Blending Constraints .....	249
10.7 Fractional or Hyperbolic Programming .....	249
10.8 Multi-Level Blending: Pooling Problems.....	250

10.9 Problems.....	255
<b>11.....</b>	<b>267</b>
<b>Formulating and Solving Integer Programs .....</b>	<b>267</b>
11.1 Introduction.....	267
11.1.1 Types of Variables .....	267
11.2 Exploiting the IP Capability: Standard Applications.....	268
11.2.1 Binary Representation of General Integer Variables .....	268
11.2.2 Minimum Batch Size Constraints .....	268
11.2.3 Fixed Charge Problems .....	269
11.2.4 The Simple Plant Location Problem .....	269
11.2.5 The Capacitated Plant Location Problem (CPL).....	271
11.2.6 Modeling Alternatives with the Scenario Approach .....	273
11.2.7 Linearizing a Piecewise Linear Function, Discontinuous Case .....	274
11.2.8 Linearizing a Piecewise Linear Function, Continuous Case.....	276
11.2.9 An $n$ Interval Piecewise Linear Function Using $\log(n)$ Binaries.....	279
11.2.10 Converting Multivariate Functions to Separable Functions .....	280
11.3 Outline of Integer Programming Methods .....	281
11.4 Computational Difficulty of Integer Programs .....	284
11.4.1 NP-Complete Problems .....	285
11.5 Problems with Naturally Integer Solutions and the Prayer Algorithm.....	286
11.5.1 Network LPs Revisited .....	286
11.5.2 Integral Leontief Constraints .....	286
11.5.3 Example: A One-Period MRP Problem.....	287
11.5.4 Transformations to Naturally Integer Formulations .....	289
11.6 The Assignment Problem and Related Sequencing and Routing Problems.....	291
11.6.1 Example: The Assignment Problem .....	291
11.6.2 The Traveling Salesperson Problem .....	293
11.6.3 Capacitated Multiple TSP/Vehicle Routing Problems.....	300
11.6.4 Minimum Spanning Tree.....	303
11.6.5 The Linear Ordering Problem .....	304
11.6.6 Quadratic Assignment Problem .....	306
11.7 Problems of Grouping, Matching, Covering, Partitioning, and Packing .....	310
11.7.1 Formulation as an Assignment Problem.....	311
11.7.2 Matching Problems, Groups of Size Two .....	311
11.7.3 Groups with More Than Two Members .....	314
11.7.4 Groups with a Variable Number of Members, Assignment Version .....	317
11.7.5 Groups with A Variable Number of Members, Packing Version .....	318
11.7.6 Groups with A Variable Number of Members, Cutting Stock Problem .....	321
11.7.7 Groups with A Variable Number of Members, Vehicle Routing.....	325
11.8 Linearizing Products of Variables .....	329
11.8.1 Example: Bundling of Products.....	330
11.9 Representing Logical Conditions.....	332
11.10 Problems.....	333
<b>12.....</b>	<b>343</b>
<b>Decision making Under Uncertainty and Stochastic Programs .....</b>	<b>343</b>
12.1 Introduction.....	343
12.1.1 Identifying Sources of Uncertainty.....	344

12.2 The Scenario Planning (SP) Approach .....	345
12.2.1 Formulation and Structure of an SP Problem .....	345
12.3 Single Stage Decisions Under Uncertainty .....	347
12.3.1 The News Vendor Problem .....	347
12.3.2 Multi-product Inventory with Repositioning .....	350
12.4 Multi-Stage Decisions Under Uncertainty .....	353
12.4.1 Stopping Rule and Option to Exercise Problems .....	354
12.4.2. An Option Exercise Stopping Problem .....	357
12.5 Expected Value of Perfect Information (EVPI) .....	358
12.6 Expected Value of Modeling Uncertainty .....	358
12.6.1 Certainty Equivalence .....	358
12.7 Risk Aversion .....	359
12.7.1 Downside Risk .....	360
12.7.2 Example .....	361
12.8 Dynamic Programming and Financial Option Models .....	364
12.8.1 Binomial Tree Models of Interest Rates .....	365
12.8.2 Binomial Tree Models of Foreign Exchange Rates .....	369
12.9 Decisions Under Uncertainty with an Infinite Number of Periods .....	371
12.9.1 Example: Cash Balance Management .....	373
12.10 Chance-Constrained Programs .....	376
12.11 Problems .....	377
<b>13.....</b>	<b>379</b>
<b>Portfolio Optimization.....</b>	<b>379</b>
13.1 Introduction .....	379
13.2 The Markowitz Mean/Variance Portfolio Model .....	379
13.2.1 Example .....	380
13.3 Dualing Objectives: Efficient Frontier and Parametric Analysis .....	383
13.3.1 Portfolios with a Risk-Free Asset .....	383
13.3.2 The Sharpe Ratio .....	386
13.4 Important Variations of the Portfolio Model .....	387
13.4.1 Portfolios with Transaction Costs .....	388
13.4.2 Example .....	388
13.4.3 Portfolios with Taxes .....	390
13.4.4 Factors Model for Simplifying the Covariance Structure .....	392
13.4.5 Example of the Factor Model .....	393
13.4.6 Scenario Model for Representing Uncertainty .....	394
13.4.7 Example: Scenario Model for Representing Uncertainty .....	395
13.5 Measures of Risk other than Variance .....	397
13.5.1 Value at Risk (VaR) .....	398
13.5.2 Example of VaR .....	398
13.5.3 VaR Anomalies .....	400
13.5.4 Conditional Value at Risk (CVaR) .....	401
13.6 Scenario Model and Minimizing Downside Risk .....	403
13.6.1 Semi-variance and Downside Risk .....	404
13.6.2 Downside Risk and MAD .....	406
13.6.3 Scenarios Based Directly Upon a Covariance Matrix .....	406
13.7 Hedging, Matching and Program Trading .....	408

13.7.1 Portfolio Hedging .....	408
13.7.2 Portfolio Matching, Tracking, and Program Trading .....	408
13.8 Methods for Constructing Benchmark Portfolios .....	409
13.8.1 Scenario Approach to Benchmark Portfolios .....	412
13.8.2 Efficient Benchmark Portfolios .....	414
13.8.3 Efficient Formulation of Portfolio Problems .....	415
13.9 Cholesky Factorization for Quadratic Programs .....	417
13.10 Positive Definiteness Constraints .....	419
13.11 Problems .....	420
<b>14.....</b>	<b>423</b>
<b>Multiple Criteria and Goal Programming .....</b>	<b>423</b>
14.1 Introduction .....	423
14.1.1 Alternate Optima and Multicriteria .....	424
14.2 Approaches to Multi-criteria Problems .....	424
14.2.1 Pareto Optimal Solutions and Multiple Criteria .....	424
14.2.2 Utility Function Approach .....	424
14.2.3 Trade-off Curves .....	425
14.2.4 Example: Ad Lib Marketing .....	425
14.3 Goal Programming and Soft Constraints .....	428
14.3.1 Example: Secondary Criterion to Choose Among Alternate Optima .....	429
14.3.2 Preemptive/Lexico Goal Programming .....	431
14.4 Minimizing the Maximum Hurt, or Unordered Lexico Minimization .....	434
14.4.1 Example .....	435
14.4.2 Finding a Unique Solution Minimizing the Maximum .....	435
14.5 Identifying Points on the Efficient Frontier .....	440
14.5.1 Efficient Points, More-is-Better Case .....	440
14.5.2 Efficient Points, Less-is-Better Case .....	442
14.5.3 Efficient Points, the Mixed Case .....	444
14.6 Comparing Performance with Data Envelopment Analysis .....	445
14.7 Problems .....	450
<b>15.....</b>	<b>453</b>
<b>Economic Equilibria and Pricing .....</b>	<b>453</b>
15.1 What is an Equilibrium? .....	453
15.2 A Simple Simultaneous Price/Production Decision .....	454
15.3 Representing Supply & Demand Curves in LPs .....	455
15.4 Auctions as Economic Equilibria .....	459
15.5 Multi-Product Pricing Problems .....	463
15.6 General Equilibrium Models of An Economy .....	467
15.7 Transportation Equilibria .....	469
15.7.1 User Equilibrium vs. Social Optimum .....	473
15.8 Equilibria in Networks as Optimization Problems .....	475
15.8.1 Equilibrium Network Flows .....	477
15.9 Problems .....	479
<b>16.....</b>	<b>483</b>
<b>Game Theory and Cost Allocation .....</b>	<b>483</b>
16.1 Introduction .....	483
16.2 Two-Person Games .....	483

x Table of Contents

16.2.1 The Minimax Strategy .....	484
16.3 Two-Person Non-Constant Sum Games .....	486
16.3.1 Prisoner's Dilemma .....	487
16.3.2 Choosing a Strategy .....	488
16.3.3 Bimatrix Games with Several Solutions .....	491
16.4 Nonconstant-Sum Games Involving Two or More Players .....	493
16.4.1 Shapley Value .....	495
16.5 The Stable Marriage/Assignment Problem .....	495
16.5.1 The Stable Room-mate Matching Problem .....	499
16.6 Should We Behave Non-Optimally to Obtain Information? .....	501
16.7 Problems .....	502
<b>17.....</b>	<b>505</b>
<b>Inventory, Production, and Supply Chain Management .....</b>	<b>505</b>
17.1 Introduction .....	505
17.2 One Period News Vendor Problem .....	505
17.2.1 Analysis of the Decision .....	506
17.3 Multi-Stage News Vendor .....	508
17.3.1 Ordering with a Backup Option .....	511
17.3.2 Safety Lotsize .....	513
17.3.3 Multiproduct Inventories with Substitution .....	514
17.4 Economic Order Quantity .....	518
17.5 The Q,r Model.....	519
17.5.1 Distribution of Lead Time Demand .....	519
17.5.2 Cost Analysis of Q,r .....	519
17.6 Base Stock Inventory Policy .....	524
17.6.1 Base Stock — Periodic Review .....	525
17.6.2 Policy.....	525
17.6.3 Analysis.....	525
17.6.4 Base Stock — Continuous Review .....	527
17.7 Multi-Echelon Base Stock, the METRIC Model.....	527
17.8 DC With Holdback Inventory/Capacity .....	531
17.9 Multiproduct, Constrained Dynamic Lot Size Problems .....	533
17.9.1 Input Data.....	534
17.9.2 Example .....	535
17.9.3 Extensions .....	540
17.10 Problems.....	541
<b>18.....</b>	<b>543</b>
<b>Design &amp; Implementation of Service and Queuing Systems .....</b>	<b>543</b>
18.1 Introduction .....	543
18.2 Forecasting Demand for Services .....	543
18.3 Waiting Line or Queuing Theory.....	544
18.3.1 Arrival Process .....	545
18.3.2 Queue Discipline.....	546
18.3.3 Service Process .....	546
18.3.4 Performance Measures for Service Systems .....	546
18.3.5 Stationarity .....	547
18.3.6 A Handy Little Formula .....	547

18.3.7 Example .....	547
18.4 Solved Queuing Models .....	548
18.4.1 Number of Outbound WATS lines via Erlang Loss Model .....	549
18.4.2 Evaluating Service Centralization via the Erlang C Model .....	550
18.4.3 A Mixed Service/Inventory System via the M/G/ $\infty$ Model .....	551
18.4.4 Optimal Number of Repairmen via the Finite Source Model .....	552
18.4.5 Selection of a Processor Type via the M/G/1 Model .....	553
18.4.6 Multiple Server Systems with General Distribution, M/G/c & G/G/c .....	555
18.5 Critical Assumptions and Their Validity .....	557
18.6 Networks of Queues .....	557
18.7 Designer Queues .....	559
18.7.1 Example: Positive but Finite Waiting Space System .....	559
18.7.2 Constant Service Time. Infinite Source. No Limit on Line Length .....	562
18.7.3 Example Effect of Service Time Distribution .....	562
18.8 Problems .....	565
<b>19.....</b>	<b>567</b>
<b>Design &amp; Implementation of Optimization-Based Decision Support Systems .....</b>	<b>567</b>
19.1 General Structure of the Modeling Process .....	567
19.1.1 Developing the Model: Detail and Maintenance .....	568
19.2 Verification and Validation .....	568
19.2.1 Appropriate Level of Detail and Validation.....	568
19.2.2 When Your Model & the RW Disagree, Bet on the RW .....	569
19.3 Separation of Data and System Structure .....	570
19.3.1 System Structure .....	570
19.4 Marketing the Model .....	571
19.4.1 Reports.....	571
19.4.2 Report Generation in LINGO .....	574
19.5 Reducing Model Size.....	576
19.5.1 Reduction by Aggregation.....	577
19.5.2 Reducing the Number of Nonzeroes .....	580
19.5.3 Reducing the Number of Nonzeroes in Covering Problems.....	580
19.6 On-the-Fly Column Generation .....	582
19.6.1 Example of Column Generation Applied to a Cutting Stock Problem .....	583
19.6.2 Column Generation and Integer Programming.....	589
19.6.3 Row Generation .....	590
19.7 Problems.....	591
<b>References .....</b>	<b>593</b>
<b>INDEX .....</b>	<b>603</b>



# Preface

This book shows how to use the power of optimization, sometimes known as mathematical programming, to solve problems of business, industry, and government. The intended audience is students of business, managers, and engineers. The major technical skill required of the reader is to be comfortable with the idea of using a symbol to represent an unknown quantity.

This book is one of the most comprehensive expositions available on how to apply optimization models to important business and industrial problems. If you do not find your favorite business application explicitly listed in the table of contents, check the very comprehensive index at the back of the book.

There are essentially three kinds of chapters in the book:

1. introduction to modeling (chapters 1, 3, 4, and 19),
2. solving models with a computer (chapters 2, 5), and
3. application specific illustration of modeling with LINGO (chapters 6-18).

Readers completely new to optimization should read at least the first five chapters. Readers familiar with optimization, but unfamiliar with LINGO, should read at least chapters 2 and 5. Readers familiar with optimization and familiar with at least the concepts of a modeling language can probably skip to chapters 6-18. One can pick and choose from these chapters on applications. There is no strong sequential ordering among chapters 6-18, other than that the easier topics are in the earlier chapters. Among these application chapters, chapters 11 (on integer programming), and 12 (on stochastic programming) are worthy of special mention. They cover two computationally intensive techniques of fairly general applicability. As computers continue to grow more powerful, integer programming and stochastic programming will become even more valuable. Chapter 19 is a concluding chapter on implementing optimization models. It requires some familiarity with the details of models, as illustrated in the preceding chapters.

There is a natural progression of skills needed as technology develops. For optimization, it has been:

- 1) Ability to solve the models: 1950's
- 2) Ability to formulate optimization models: 1970's
- 3) Ability to use turnkey or template models: 1990's onward.

This book has no material on the mathematics of solving optimization models. For users who are discovering new applications, there is a substantial amount of material on the formulation of optimization models. For the modern "two minute" manager, there is a big collection of "off-the-shelf", ready-to-apply template models throughout the book.

Users familiar with the text *Optimization Modeling with LINDO* will notice much of the material in this current book is based on material in the LINDO book. The major differences are due to the two very important capabilities of LINGO: the ability to solve nonlinear models, and the availability of the set or vector notation for compactly representing large models.

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